INCIDENT DETECTION USING A FUZZY-BASED NEURAL NETWORK MODEL

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Abstract: Incidents on the freeway disrupt traffic flow and the cost of delay caused by the incidents is significant. To reduce the impact of an incident a traffic management center needs to quickly detect and remove it from the freeway. In this vein quick and efficient automatic incident detection has been the main goal of the transportation research for many years. Also many algorithms based on loop detector data have been developed and tested for automatic incident detection. However, many of them have a limited success in their overall performance in terms of detection rate, false alarm rate, and the mean time to detect an incident. The objective of this paper is to propose a robust and reliable method for detecting an incident on the freeway using a fuzzy based neural network model, Fuzzy ARTMAP which is a supervised, self-organizing system claimed to be more powerful than many expert systems, genetic algorithms, or other neural network models like Backpropagation. The experiments have been done with simulated data, and the results show that Fuzzy ARTMAP has the potential for the application of automatic incident detection in the real world, where a large number of incident data is not always available for training.

Key Words: Incident detection, Backpropagation, Fuzzy ARTMAP

1. INTRODUCTION

An incident is non-recurrent event that causes a severe reduction or an abnormal increase in the demand of a transportation facility. The function of Automotive Incident Detection (AID) is to automatically identify the occurrence of unpredictable incidents that affect the capacity of freeways so that appropriate response and clearance procedures can be executed to minimize the effects of the incident on traffic operation. Since the 1970s, there has been growing interest in the incident detection, and a variety of algorithms have been developed (Dudek, *et al.* 1974; Ahmed and Cook, 1982; Busch and Fellendorf, 1990; Chassiakos, *et al.* 1993). Unfortunately, the algorithms developed to date have had only limited operational success, and it is clear that improved algorithms are needed to make loop data based incident detection technology operationally effective. Specifically, existing algorithms have been largely ineffective in maintaining the high degree of reliability required in practice (e.g., high detection rate and low false alarm rate).

In order to achieve the better performance on the incident detection, some researches (Ritchie and Cheu, 1993; Payne, Payne and Thompson, 1997) have used Artificial Neural Networks which hold considerable potential for recognizing and classifying spatial and temporal patterns in traffic data. The findings of previous researches indicates that neural network models have the potential to achieve significantly better performance in terms of detection rate and false alarm rate, as well as operational improvements in real-time incident detection over more conventional algorithms such as a series of California algorithms and McMaster algorithm(Hall, *et al.*, 1993).

Even though there are currently many different types of neural network models available, the multilayer feedforward with backpropagation learning algorithm, usually called Backpropagation (Rumelhart, *et al.* 1986), has been the most popular neural network for the incident detection. However, the Fuzzy ARTMAP(Carpenter *et al.*, 1992) has been claimed to have better performance than the Backpropagation, in terms of predictive accuracy, in experiments with benchmark data (Carpenter *et al.*, 1994 a, 1994b) and with signal processing data (Young, 1995). For the automatic incident detection, Fuzzy ART(Carpenter *et al.*, 1991a), the previous version of Fuzzy ARTMAP, has been used and shown to have better performance than the Backpropagation(Ishak, 1999).

In this research, Fuzzy ARTMAP(Carpenter *et al*, 1992) has been applied for automatic incident detection. The network performance of the Fuzzy ARTMAP has been compared with the results of the Backpropagation to investigate how the network performance, in terms of detection rate and false alarm rate, would be different. Another important issue in this research is to see how the number of incident and non-incident data sets available for training would effect the network performance on two different neural network models.

2. BACKPROPAGATION AND FUZZY ARTMAP

Backpropagation is an error-correcting learning procedure that generalizes the delta rule (Rumelhart et al., 1986a) to multilayer feedforward neural networks with hidden neurons between the input and output vectors. Up to now, feedforward network with the error backpropagation learning rule has been the most popular neural network. It has been applied in various problems successfully. However, there remain some problems associated with their use. First, Backpropagation can only learn slowly in an off-line setting with an essentially stationary environment (Carpenter, 1989; Grossberg, 1987; Rumelhart et al., 1986). Second, the computing cost for training in the Backpropagation is very high. Even though the computing cost is not currently high with rapid improvement of computer technology, it may still be a problem when we deal with a large number of data sets and input units. Third, There is no rule for the proper selection of the network topology. The number of hidden units to use in the hidden layer(s) cannot be easily determined beforehand. Fourth, there is the possibility of being trapped at a local minimum during the training process, preventing the network from converging to a more desirable error value. Gradient descent methods are in general very susceptible to local minima and flat spots, and the Backpropagation algorithm is not immune to this. Despite the unsolved issues as described above, Backpropagation has been used as a representative model with which to compare newly developed neural network model because of its popularity and a good performance on various problems.

On the other hand, Fuzzy ARTMAP has an on-line learning mechanism and the superior performance with very low computing costs for training. Fuzzy ARTMAP is a combination of

fuzzy logic and Adaptive Resonance Theory (ART). Since ART1 (Carpenter and Grossberg, 1987a) has been developed, a series of ART models, which are based on ART1 module, have been developed. They include ART2 (Carpenter and Grossberg, 1987b) which handles analogue inputs, Fuzzy ART (Carpenter *et al.*, 1991a) which incorporates computations from fuzzy set theory in to ART1 model, ARTMAP (Carpenter *et al.*, 1991b) which is supervised learning system on ART modules, and Fuzzy ARTMAP which is supervised learning system and achieves a synthesis of fuzzy logic and ART neural network.

Fuzzy ARTMAP consists of two fuzzy ART modules, ART_a and ART_b , connected by an inter-ART module, F^{ab} , called the map field. ART_a and ART_b create stable recognition categories in response to arbitrary sequences of input patterns. Each module receives either the input or output component of each pattern pair to be associated. The main function of the map field is to associate representations of the pattern pair components. When there is mismatch between the prediction by ART_a and actual ART_b input, the map filed subsystem, *match tracking*, is activated, The *match tracking* raises the ART_a vigilance ρ_a by just the amount needed to cause a mismatch and reset in the ART_a module. Then, the ART_a search system is activated to have either an ART_a category that correctly predicts an actual ART_b input or a previously uncommitted ART_a category node. The algorithm can be summarized as follows:

Summary of Fuzzy ARTMAP Algorithm

Step 0. Let *m* be the number of input units, *n* be the number of output units, *M* be the number of units on F_2^a , and *N* be the number of units on F_2^b .

Initially, all the adaptive weights W_j^a , W_k^b and W_{jk}^{ab} are set equal to 1, i.e.

$$\mathbf{W}_{j1}^{a}(0) = ... = \mathbf{W}_{j2m}^{a}(0) = 1$$
 $\mathbf{W}_{k1}^{b}(0) = ... = \mathbf{W}_{k2n}^{b}(0) = 1$
 $\mathbf{W}_{jk}^{ab}(0) = 1$
where $j = 1, ..., M$ and $k = 1, ..., N$

Initialize all category nodes of ART modules, ART_a and ART_b, by making them *uncommitted*. Set the parameters: the choice parameter $\alpha > 0$; the learning rate parameter $\beta \in [0,1]$; and the vigilance parameters ρ_a , ρ_b , $\rho_{ab} \in [0,1]$. Set the ART_a vigilance parameter, ρ_a , to the baseline vigilance, $\overline{\rho_a}$.

Step 1. Present a binary or analogue vector \mathbf{a} and the corresponding class vector \mathbf{b} . The vector \mathbf{a} is input to module ART_a and the vector \mathbf{b} is input to module ART_b. All input values of vector \mathbf{a} must be within the range [0,1]. If not, i.e. the inputs to the ART_a are analogue, then the input vector \mathbf{a} should be normalized (Kim, 1999a for more details in normalization). The complement coding is also required to preserve amplitude information, then the complement coded input vector $\mathbf{A} = (\mathbf{a}, \mathbf{a}^c) = (a_1, \dots a_m, a_1^c, \dots, a_m^c)$ is input to the field \mathbf{F}_1^a and the input vector $\mathbf{B} = (\mathbf{b}, \mathbf{b}^c) = (\mathbf{b}_1, \dots \mathbf{b}_n, \mathbf{b}_1^c, \dots, \mathbf{b}_n^c)$ to the field \mathbf{F}_1^b . These are 2m -dimensional and 2n-dimensional vectors respectively. Complement coding and normalization of input vectors solve the category proliferation problem (Carpenter *et al*, 1991).

Step 2. For each input **A** and **B**, the j^{th} node in the layer, F_2^a , and k^{th} node in the layer, F_2^b , are given by

$$T_{j}(\mathbf{A}) = \frac{\left|\mathbf{A} \wedge \mathbf{W}_{j}^{a}\right|}{\alpha + \left|\mathbf{W}_{j}^{a}\right|} \text{ and } T_{k}(\mathbf{B}) = \frac{\left|\mathbf{B} \wedge \mathbf{W}_{k}^{b}\right|}{\alpha + \left|\mathbf{W}_{k}^{b}\right|},$$

where the fuzzy MIN operator \wedge is defined to be $(x \wedge y)_i = \min(x_i, y_i)$, α is a choice parameter, and the norm $|\cdot|$ is defined to be $|\mathbf{x}| = \sum_i |x_i|$ for any vectors \mathbf{x} and \mathbf{y} .

Step 3. Use a winner-take-all rule to select the winner. This yields the maximum weighted sum. The winners of ART_a and ART_b are indexed by J and K respectively, where

$$J = \max\{T_j(A): j = 1,..., M\}$$
 and $K = \max\{T_k(B): k = 1,..., N\}$

If more than one node is maximal on each module, the node with the smallest index is chosen to break the tie.

Step 4. Check the vigilance criteria. If nodes *J* and *K* satisfy the conditions

$$\frac{\left|\mathbf{A} \wedge \mathbf{W}_{\mathtt{J}}^{\mathtt{a}}\right|}{|\mathbf{A}|} \geq \rho_{a} \text{ and } \frac{\left|\mathbf{B} \wedge \mathbf{W}_{\mathtt{K}}^{\mathtt{b}}\right|}{|\mathbf{B}|} \geq \rho_{b}$$

then nodes J and K are chosen to represent the input patterns \mathbf{A} and \mathbf{B} , and proceed to Step 5. After the categories represented by nodes J and K are selected for learning, they become *committed*. If they violate the above condition, then node J and K are reset, and move back to Step 3. Search for another node in the F_2^a and F_2^b that satisfies vigilance criterion respectively.

Step 5. Check to see whether the match tracking criterion is satisfied. If

$$\frac{\left|\mathbf{y}^{b} \wedge \mathbf{W}_{J}^{ab}\right|}{\left|\mathbf{y}^{b}\right|} \ge \rho_{ab}$$

then we have achieved the desired mapping and continue to Step 6 for LTM (Long Term Memory) learning. If

$$rac{\left|\mathbf{y}^{b}\wedge\mathbf{W}_{J}^{ab}
ight|}{\left|\mathbf{y}^{b}
ight|}\langle
ho_{ab}$$

then the mapping between J and K is not the desired one. In this case, the vigilance parameter ρ_a is increased until it is slightly larger than $|\mathbf{A} \wedge \mathbf{W}_J^a|/|\mathbf{A}|$; this leads to an immediate reset of node J in ART_a and a move to Step 3 with the new vigilance parameter for the selection of another node in F_2^a that will achieve the desired mapping.

Step 6. The weights \mathbf{W}_{L}^{a} and \mathbf{W}_{K}^{b} are updated by the equations

$$\mathbf{W}_{J}(t) = \beta(\mathbf{A} \wedge \mathbf{W}_{J}(t-1)) + (1-\beta)\mathbf{W}_{J}(t-1)$$
 and

$$\mathbf{W}_{K}(t) = \beta(\mathbf{A} \wedge \mathbf{W}_{K}(t-1)) + (1-\beta)\mathbf{W}_{K}(t-1)$$

, where the learning rate β is chosen in the range [0,1]. In the *fast learning* mode, β is set to 1. The weights \mathbf{W}_{j}^{a} , $j \neq J$ and \mathbf{W}_{k}^{b} , $k \neq K$ of non-winning nodes are not updated. For efficient

coding of noisy input sets, *fast-commit and slow recording*, which is to set $\beta = 1$ when J is an uncommitted node and take $\beta < 1$ after the category committed, is normally being used.

Map field weights with fast learning are determined by

$$\mathbf{W}_{jk}^{ab}(t) = \begin{cases} 1 & \text{if } j = J, \ k = K \\ 0 & \text{if } j = J, \ k \neq K \\ \mathbf{W}_{jk}^{ab}(t-1) & \text{otherwise} \end{cases}$$

Step 7. Go to Step 1 and present a next pattern pair.

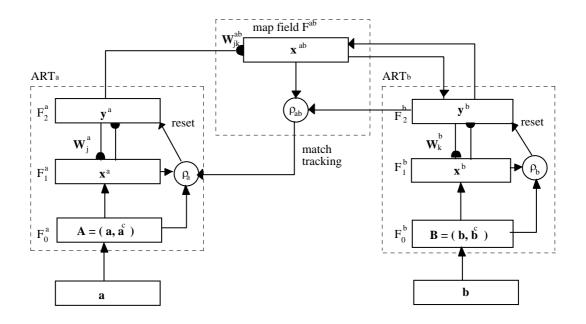


Figure 1. Fuzzy ARTMAP Architecture

3. EXPERIMENT AND RESULTS

3.1. Experimental Data

Traffic flow parameters associated with an incident can be quantitatively expressed by values of traffic flow characteristics such as traffic volume, speed and occupancy. In automatic incident detection algorithms, these variables have been used as useful information and abrupt changes have activated the incident warning system.

Even though incident and incident-free traffic data are currently available from the loop detectors installed on freeways, data are not reliable because of the malfunction of detectors and network disconnection. More importantly, it is very difficult to get exact incident data regarding incident time and location in the real world. In this research, simulation data, which was obtained by using traffic simulator, INTEGRATION, to obtain incident and incident-free

traffic flow data. The INTEGRATION traffic simulator provides three major traffic parameters, volume, speed and occupancy. However, the recorded occupancy in this simulator is computed as a function of a derived density(volume/speed) and the detection length. For this reason, only volume and speed can be useful for experiments, even though occupancy is an important measurement for an automatic incident detection system.

Figure 2 shows the location of detectors and an incident occurrence on the two lanes of the freeway. Detector stations 1 through 3 are located on the eastbound freeway and positioned 2.5 km, 3 km and 3.5 km from the upstream end of the link. It is assumed that the incident blocks the median lane starting at a location 3.2 km from the upstream end of the link. In order to represent various traffic flow situations from the free flow to the congested flow in the experiments, the O-D demand for traffic generation ranges from 1000pc/h/ln to 2500pc/h/ln.

The input data for the application of Neural Network models are average speed and volume measurements recorded at each station during every 30 seconds of polling cycle. The traffic volume and speed from the median lane detector in Station 2 are zero when the incident blocked the median lane. This means that a simple detection system could detect an incident in very easily with the extreme value of traffic parameters. For the study, an average speed and volume for each station has been used to develop more a reliable detection system, which may distinguish incident traffic flow from recurrent traffic congestion.

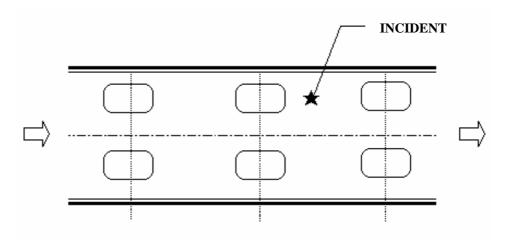


Figure 2. Loop Detector Locations and Incident Occurrence

Table 1 represents the number of incident and incident-free data which have been used for training and testing. In this study, four different experiments have been done to see the network performance in terms of the incident detection according to the number of incident and incident-free data sets for training.

For the application of Backpropagation, the training sets size of 120 on the Exp. 4 is much smaller than the suggested by Baum and Haussler (1989) and *Widrow's rule of thumb* (Widrow, 1987). The experimental results show that this rule is not always acceptable (Kim, 1999b).

Test data Training data Exp. 2 Exp. 3 Exp. 4 Exp. 1 Incident 250 400 125 60 60 Incident-Free 120 120 120 60 180 Total 370 245 180 120 580

Table 1. The Number of Data Sets For Training and Testing

3.2. Experiment and Results

In this study, all experiments with the standard Backpropagation network were implemented on the three-layer network with 25 hidden neurons, 6-25-1. The input vector property is the average 30-seconds volume and the speed between two detectors at each detector station. The network has been learned with a learning rate of 0.01 and a sequential learning mode, since the sequential learning mode is much more efficient than the batch mode learning (Kim, 1999b). The error goal of a RMSE(Root Mean Squared Error) for stopping network training was approximately 0.1.

In comparison, the Fuzzy ARTMAP parameters used for the simulation are shown on the Table 2. The ART_a baseline vigilance is set to 0, and the ART_b baseline vigilance is set to 1, i.e. $\overline{\rho_a} = 0$ and $\overline{\rho_b} = 1$. The input for the ART_b module is the pattern category, which we need to learn and predict correctly, corresponding to the output vectors of the supervised neural network model, as in the Backpropagation network. In order to achieve the maximum generalization for the training patterns, the baseline vigilance of ART_a is set to 0. If the ART_a baseline vigilance is set to the high value initially, the generalization will be very low since those patterns which are only slightly different will have their own winning vector on the F_2^a . For the learning algorithm, *fast-commit and slow recording* is used with a learning rate parameter $\beta = 0.001$ for all experiments in this research. For the experiment in this research, 5 votes have been used.

In terms of computing cost for training, Fuzzy ARTMAP is superior to the standard Backpropagation. Table 3 shows the performance in terms of prediction accuracy of two different neural network models on the incident and incident-free test data sets. The prediction accuracy of Fuzzy ARTMAP on the test data sets ranges from 89.1% to 91.6% according to the number of training data set. For Backpropagation, it ranges from 83.4% to 93.6%.

For the Exp. 1 and 2 which have been trained with a large number of incident-free and incident data sets, Backpropagation produced a little better performance in terms of detection rate than the Fuzzy ARTMAP. However, for the small number of incident and incident-free data sets as on Exp. 4, Fuzzy ARTMAP yields much better performance than Backpropagation.

Even though some previous research showed the better performance of Fuzzy ARTMAP compare to Backpropagation, this paper shows that the network performance can be vary

according to the number of training set size. The experimental results show that the Fuzzy ARTMAP algorithm may produce better performance than Backpropagation in terms of detection rate and false alarm rate, especially with small numbers of incident data sets available. Otherwise, Backpropagation would be more efficient than the Fuzzy ARTMAP. In addition, Fuzzy ARTMAP may be much efficient when training data sets are significantly different since it has the ability of a network to learn patterns without forgetting the old ones, i.e. Fuzzy ARTMAP can recognize any significantly different new pattern as well as the previously trained ones. There is, however, a need to retrain the network with the new pattern plus all of the previous patterns in order to recognize new patterns for Backpropagation. This process may effect the previously trained ones seriously if it is significantly different from old ones.

Table 2. Fuzzy ARTMAP Parameters Used for the Simulation

Parameter	Description
$\epsilon = 0.001$	Match tracking parameter (increase ART _a vigilance)
$\alpha = 0.001$	Choice parameter for the search order of fuzzy ART
	modules
$\beta_a = 0.001$	Fuzzy ART _a learning rate
$\beta_b = 1.0$	Fuzzy ART _b learning rate
$\beta_{ab} = 1.0$	Map field learning rate
$\overline{\rho}_a = 0.0$	Baseline Fuzzy ART _a vigilance
$\rho_b = 1.0$	Baseline Fuzzy ART _b vigilance
$\rho_{ab} = 1.0$	Map Field vigilance

Table 3. Performance on the two neural network models

Performance	Exp. 1 ¹⁾		Exp. 2^{2}		Exp. 3 ³⁾		Exp. 4 ⁴⁾	
	BP	F.A	BP	F.A	BP	F.A	BP	F.A
Errors on Incident-free	12/180	16/180	25/180	22/180	26/180	33/180	26/180	25/180
data								
Errors on Incident data	25/400	45/400	24/400	28/400	66/400	20/400	70/400	36/400
Total error (%)	37/580	61/580	49/580	50/580	92/580	53/580	96/580	63/580
	(6.4%)	(10.5%)	(8.4%)	(8.6%)	(15.9%)	(9.1%)	(16.6%)	(10.9%)
Detection Rate(%)	93.8	88.8	94.0	93.0	83.5	95.0	82.5	91.0
False Alarm Rate(%)	6.7	8.9	13.9	12.2	14.4	18.3	14.4	13.9

¹⁾ Experiment has been done with 250 for incident-free and 120 for incident training data sets

²⁾ Experiment has been done with 125 for incident-free and 120 for incident training data sets

³⁾ Experiment has been done with 60 for incident-free and 120 for incident training data sets

⁴⁾ Experiment has been done with 60 for incident-free and 60 for incident training data sets

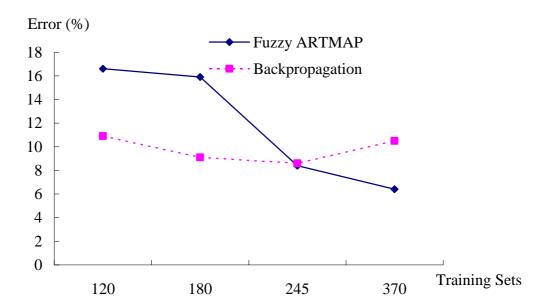


Figure 3. Performance with Different Training Set Size

4. CONCLUSIONS

In this research, a fuzzy-based neural network model, Fuzzy ARTMAP, has been explored for incident detection. The performance of Fuzzy ARTMAP was found to be competitive with the Backpropagation which has been the most popular neural network for the incident detection in terms of the detection rate and the false alarm rate. In the real world, it is difficult to obtain a large number of incident and non-incident data sets for training and so the Fuzzy ARTMAP could be more reliable especially when the small numbers of training data sets are available.

In addition, the Fuzzy ARTMAP has a built-in mechanism for the network to be able to recognize the novelty of the input, if a previously unseen input pattern is introduced. As a result, if there is significantly different types of incident and incident-free traffic parameter data are given, then the Fuzzy ARTMAP would be much more efficient than any other neural network models. However, if a large number of training sets for incident and incident-free data are available and the noise on the real world data is not serious, Backpropagation could be much more efficient because of its powerful generalization.

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